Image Registration Underwater for Fluid Flow Measurements and Mosaicking

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Abstract - In this paper we present a unified framework of increasing complexity that handles image registration ranging from translation only motion between images, to a full eight parameter projective transformation. Our formulation deals specifically with the constraints that are peculiar to these applications underwater. To examine the role of translation only motion across images we look at video imagery from fluid flow across a flange at a hydrothermal vent site in Guaymas Basin in Mexico. We then show the extensions to this algorithm that are required to handle the case for 2D mosaicing, which involves translations, rotations, scale, and shear in an unstructured three dimensional underwater world. Finally, we show the effectiveness of these techniques on data acquired during photographic surveys of an ancient Roman shipwreck located in the Skerki Bank region in ~800m of water in the Mediterranean.

Introduction
From its modest beginnings in the 1890s with the work of Louis Baton in the French Riviera, underwater photography has progressed to become an important tool in deep sea research[1]. With the loss of the nuclear powered submarine the USS Thresher in 1963 came a surge of interest in deep sea photographic equipment and techniques that has eventually led to the routine use of photomosaicking in an underwater context. The early techniques employed film and used rectifying lenses that reprojected images to allow the merging of multiple images into a composite mosaic. Numerous examples of the use of these techniques exist today including mosaics of the Monitor[2], the Thresher[2], and of geological sites of interest photographed during project Famous[3].

With the advent of digital computers and CCD cameras in the late 1980s, efforts at the Deep Submergence Laboratory (DSL) of the Woods Hole Oceanographic Institution (WHOI) have focused on using specialized image processing hardware for manipulating and processing digital images of underwater scenes to manually construct photomosaics[4][5]. Work on underwater photomosaicking is currently also being pursued at other institutions[6][7][8].

Independent of the work being carried out underwater, photomosaicking is routinely used for satellite imagery[9] as well as for mobile land robots[10][11][12][13]. Although these fields have reported significant advances, there are fundamental differences between these applications and the underwater domain. The chief differences are in the area of lighting and in the unstructured three dimensional nature of the underwater terrain. Thus, we focus in this paper on these differences and the techniques involved in addressing these differences to build large area photomosaics underwater.

2D Translation & Fluid Flow
Beginning with the simplest case, the following describes the mathematics behind image registration of pure translation only motion between images, set in the context of an interesting application. Photomosaicking techniques were used in the summer of 1999 to make volumetric flow rate measurements of a hydrothermal vent site in Guaymas Basin, Mexico; something which had never been done before. A clear graduated cylinder was modified to have a special funnel base which directed all of the expelled hydrothermal exhaust water through the cylinder. The special base also had a dye injection system which released a continuous stream of fluorescent dye into the funnel coloring the exhaust water inside the cylinder. The remotely operated vehicle (ROV) Jason, operated by DSL at WHOI, was used to deploy this graduated cylinder device at a hydrothermal vent site and then record the fluid flow imagery onto standard video at a frame rate of 30Hz.

The concept for extracting volumetric flow rate measurements at the vent lies in the assumption that between successive frames of video, the dye in the cylinder undergoes pure translation only motion. If this translation can be found, an average velocity
measurement of the fluid can be calculated from the time between successive frames. Multiplying the average velocity by the cylinder cross-sectional area produces an average volumetric flow rate.

To recover the fluid translation through Fourier transform phase correlation techniques, the first step was to reduce the backscatter noise present in the background of the image; this was accomplished by isolating the cylinder and dye from the rest of the image as shown in Figure 1. Clearly the assumption of translation only motion is valid as frame 4-06 is seen to be merely a shifted version of frame 4-01.

Thus, defining the image in frame 4-01 to be $x_1[n_1, n_2]$, the image in frame 4-06 can be written as:

$$x_2[n_1, n_2] = x_1[n_1 - m_1, n_2 - m_2]$$  \hspace{1cm} (1)

To find the delay $m_1$ and $m_2$, begin by noting the Fourier transforms, $\mathcal{F}$, of $x_1[n_1, n_2]$ and $x_2[n_1, n_2]$:

$$\mathcal{F}(x_1[n_1, n_2]) = |X_1(j\Omega_1, j\Omega_2)| e^{\phi_x(j\Omega_1, j\Omega_2)}$$  \hspace{1cm} (2)

$$\mathcal{F}(x_2[n_1, n_2]) = \frac{|X_1(j\Omega_1, j\Omega_2)| e^{\phi_x(j\Omega_1, j\Omega_2)}}{e^{jm_1\Omega_1} e^{jm_2\Omega_2}}$$  \hspace{1cm} (3)

Multiplying $X_1(j\Omega_1, j\Omega_2)$ by the conjugate of $X_2(j\Omega_1, j\Omega_2)$ and then dividing by the magnitude of their respective product yields:

$$G(j\Omega_1, j\Omega_2) = \frac{X_1 \cdot X_2^*}{|X_1 \cdot X_2^*|} = e^{jm_1\Omega_1} e^{jm_2\Omega_2}$$  \hspace{1cm} (4)

Taking the inverse Fourier transform of $G(j\Omega_1, j\Omega_2)$ results in the spatial function $g[n_1, n_2]$,

$$g[n_1, n_2] = \delta[n_1 - m_1, n_2 - m_2]$$  \hspace{1cm} (5)

from which the translation measurements are obtained from the coordinates of the unit sample. From here, the velocity and volumetric rates are easily calculated.

**Photomosaicking**

The process of photomosaicking involves aligning multiple images to one another and then merging these images into a seamless composite representation. The alignment of a pair of images may be accomplished by a
variety of techniques which include manual tie point location, spatial techniques, and Fourier transform based methods. A good survey of image registration techniques is that by Brown[14]. These techniques vary from being very labour intensive to completely automated with attendant trade-offs in ease of use and accuracy. In particular, we look at manual tie point location and spatial techniques and their roles in the context of underwater applications.

**Manual Location of Tie Points**

We should point out that several packages exist that provide an easy to use interface that allows manual photomosaicking. Operators are presented with views of the images to be mosaicked and then select common features across these images. A linear least squares solver package is typically employed to solve the over constrained set of equations that correspond to the manually selected tie points to estimate the transformation between the pair of images.

The residuals associated with the process of solving the over constrained set of equations provides a level of quality control over the process. Typically, operators can fine-tune their choice of tie points to reject those with high residuals to produce an aesthetically pleasing mosaic.

The techniques associated with manual mosaicking have additional significance in areas with unstructured hard-to-model relief.

**Spatial Methods**

Our spatial approach to photomosaicking mirrors that of Sawhney and Kumar[10], although it differs in important ways to deal with the peculiarities of the underwater environment.

Let $I_1 \ldots I_N$ be the $N$ images that we are trying to register.

If we consider an ideal coordinate system where a point $p$ is given by $p = (x, y)$ and $p_i = (x_i, y_i)$ is the representation of that point in image $I_i$ such that the point $p$ is related to $p_i$ by the mapping

$$p_i = P(p; A_i)$$

where $A_i$ is the 3D-to-2D or 2D-to-2D projection transformation that maps $p$ to $p_i$; $A_i$ may be a Helmert, affine, projective, or higher order transformation.

For the purposes of this paper we assume $A_i$ to represent an eight parameter projective plane transformation

$$x_i = \frac{a_{11}^i x + a_{12}^i y + a_{13}^i}{a_{31}^i x + a_{32}^i y + a_{33}^i}$$

$$y_i = \frac{a_{21}^i x + a_{22}^i y + a_{23}^i}{a_{31}^i x + a_{32}^i y + a_{33}^i}$$

where $a_{11}^i$ through $a_{33}^i$ are the plane projective parameters that correspond to image $I_i$.

The correspondence between the points in the images and the coordinate transformation must both be accomplished simultaneously. The brightness constancy constraint can be used in this respect as it relates

$$I_i(p_i; (p, A_i)) = I_{i+1}(p_{i+1}; (p, A_{i+1}))$$

However, while this may serve as a good enough approximation in some cases, it is not generally applicable for underwater imagery. The light source moves with the camera on underwater imaging platforms and in the case for non-uniformly illuminated images, equation (4) does not hold true. Thus we deviate from the formulation proposed by Sawhney and Kumar in two important ways.

1. We substitute adaptively histogram equalized imagery in place of the original images even though, due to aesthetic considerations, we may use the unequalized images for the mosaic.

2. We detect and discount the contribution due to shadows. As the light source moves, the shadows tend to also shift. Due to the low contrast nature of underwater imagery, techniques which rely on edge based operators are often fooled by this apparent motion across images.

Thus if we consider the $i$th histogram equalized image $I_i^h$ and the subset $S$ of the original image $I$ such that the intensity in $S$ corresponds to shadowed regions and their neighbors, then we can minimize the error criterion,

$$\min_{A_i, A_{i+1}} \sum_{p \in S} \frac{1}{M(p)} \sum_{i, i+1} (I_i^h(p_i) - \bar{I}(p))^2$$

This can be linearized

$$E((p_i; p); A) = \frac{1}{\sqrt{M(p)}} (I_i^h(p_i) - \bar{I}(p))$$

such that each iteration of the Levenberg-Marquadt optimization procedure solves the following linear sum of squares problem .
Our implementation uses a two step progressively complex model in combination with a Laplacian of Gaussian pyramid. We first estimate the translation parameters at a coarse level of the pyramid using a scheme similar to that used for fluid flow measurements and then use those values to estimate the parameters corresponding to the projective transformation.

The results of our techniques are highlighted in Figures 2 and 3. Figure 2 shows the general methodology we follow for the photomosaicking process. Figure 3 shows a complete photomosaick of a 4th century B.C. Roman shipwreck located in ~800m of water in the Mediterranean. This photomosaic is a composite of 180 images that were assembled in four strips that were then manually assembled into a composite photomosaic.

These and other results along with the implementation of this algorithm are discussed at length in [15].

Conclusions

In this paper we have attempted to demonstrate a unified framework to photomosaicking with a particular emphasis on the unique constraints of underwater imagery. The techniques presented are general building blocks towards a global underwater image registration suite. Areas of future and on-going research here at DSL which work towards this end goal are: color histogram equalization to produce color mosaics, understanding and quantifying the effects of an unstructured 3D environment on mosaics, and finally, 3D image reconstruction from a single camera on a moving underwater platform.

\[
\left( \min_{\delta A} \sum_{p \in s} \sum_{i} (E(p_i; \delta p) + \nabla E(p_i; \delta p)[\delta A]) \right) \quad (11)
\]
Figure 3. Mosaic of a 4th Century B.C. Roman shipwreck located in ~800m of water in the Mediterranean; the mosaic was constructed from 180 images taken from the Jason ROV.
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References